

**Rationalize Denominator** means to make it rational. Square roots of non-perfect squares are irrational because they do not terminate nor do they repeat when placed in decimal form. Thus, rationalize a denominator means to simplify so that there is no  $\sqrt{\phantom{x}}$  in denominator.

### Steps to Rationalize a Denominator with One Term

1. Write out problem.
2. Simplify numerator and denominator completely.
3. If numbers outside of  $\sqrt{\phantom{x}}$  in the numerator and denominator have common factors, simplify.
4. **If a  $\sqrt{\phantom{x}}$  ends up in the denominator, multiply both numerator and denominator by  $\sqrt{\phantom{x}}$  from the denominator.**
5. When multiplying  $\sqrt{\phantom{x}}$ 's you multiply numbers under  $\sqrt{\phantom{x}}$ 's together and numbers in front of  $\sqrt{\phantom{x}}$ 's together.
6. After multiplying  $\sqrt{\phantom{x}}$ 's, simplify new  $\sqrt{\phantom{x}}$ 's and simplify numbers in front.

Examples: Simplify

$$\sqrt{\frac{7}{20}}$$

$$\frac{\sqrt{7}}{\sqrt{20}}$$

$$\frac{\sqrt{7}}{\sqrt{4 \cdot 5}}$$

$$\frac{\sqrt{7}}{\sqrt{4} \sqrt{5}}$$

$$\frac{\sqrt{7}}{2\sqrt{5}}$$

$$\frac{\sqrt{7} \cdot \sqrt{5}}{2\sqrt{5} \cdot \sqrt{5}}$$

$$\frac{\sqrt{35}}{2\sqrt{25}}$$

$$\frac{\sqrt{35}}{2 \cdot 5}$$

$$\frac{\sqrt{35}}{10}$$

A  $\sqrt{\phantom{x}}$  remains in denominator so we rationalize by multiplying numerator and denominator by the  $\sqrt{\phantom{x}}$  in the denominator.