

## Whole Numbers and Factoring

**Factors** are the numbers multiplied together to obtain a product. In the expression,  $2 \times 3 = 6$ , the numbers 2 and 3 are factors and the 6 is a product.

**Factoring** is the process of starting with a number and rewriting it as a product or factors.

**Prime** numbers are numbers greater than one and have no other factors besides one and themselves. Here is a list of prime numbers less than 30: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29

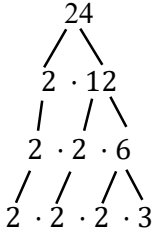
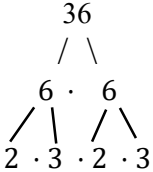
**Composite** numbers are numbers greater than one and have factors other than one and themselves. For example, 12 has factors of 1, 2, 3, 4, 6, and 12. We can write a variety of multiplication problems to obtain a product of 12.

- $1 \times 12 = 12$
- $2 \times 6 = 12$
- $3 \times 4 = 12$

A prime number, such as 17, only has factors of one and seventeen. We can only write one multiplication problem:  $1 \times 17 = 17$ .

**Prime factorization** has the final step with prime factors. Factor trees are used for prime factorization. Every row of a factor tree has products that multiply together to obtain the number on top.

Example: Use factor trees to factor 24, 19, and 36.

	<p>19 <i>prime</i></p>	
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When factoring a prime number completely with a tree, just write “prime”.

Note: Bring down **all** prime factors in factor trees. Some books show circled prime factors.

Timetables are very helpful when factoring. For large numbers, there are some basic rules to find factors.

**2** is a factor of any even number with a last digit of 0, 2, 4, 6, or 8. The number, 43,246 ends in 6 and thus it has factor of 2.

**3** is a factor any number where the digits of the number add up to a sum that has 3 as a factor. For example, the number 417 has 3 as a factor. If you add the digits of 417,  $4 + 1 + 7$ , the sum is 12. 12 has 3 as a factor and thus the original number of 417 has 3 as a factor.

**5** is a factor of any number with a last digit of 0 or 5. The number, 48,215, has a factor of 5 since it ends with 5.

**10** is a factor of any number with a last digit of 0. The number, 3490, has a factor of 10 since it ends with 10.